An Efficient of Overlapping Grid Method with Scattering Technique in Time Domain for Numerical Modeling

Bong Siaw Wee*, Kismet Hong Ping& Shafrida Sahrani*

*Department of Electrical Engineering, Politeknik Mukah, 96400 Mukah, Sarawak, Malaysia
&Department of Electrical and Electronic Engineering, Faculty of Engineering, Universiti Malaysia Sarawak, 94300 Kota Samarahan, Sarawak, Malaysia
&Institute of IR4.0, Universiti Kebangsaan Malaysia, 43600 Bangi, Selangor Malaysia

*Corresponding author: shaweibong2016@gmail.com

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ABSTRACT

An Overlapping Grid Method (OGM) with Biquadratic Spline Interpolation in scattering technique was developed to solve the direct and inverse scattering issues. A two-dimensional (2D) numerical image model was used to analyze the accuracy of the proposed method in a direct scattering process. It was discovered that when the sub-grid, $\Delta x$, increased, the absolute error for the electric field amplitude will also increase. The results also discovered that as the grid size ratio increased, the absolute error of the amplitude $E_z$ will also increase. The findings show that smaller grid spacing and a finer grid size can produce more accurate results. The Overlapping Grid Method (OGM) with Biquadratic Spline Interpolation was expanded by incorporating with Forward-Backward Time Stepping (FBTS) technique to solve inverse scattering issues. Homogenous embedded objects with a square and circular shape are used to validate the efficiency of the proposed method. The findings showed that the proposed numerical method could detect and reconstruct embedded objects in different shapes. The efficiency of the proposed method was examined by Mean Square Error (MSE) and normalizing the functional error. The findings revealed that the MSE of dielectric profiles for the proposed method were lower than the FDTD method in FBTS. The relative permittivity and conductivity profile differed by 27.06% and 20%, respectively. Hence, it was proven that the proposed method successfully solved a known drawback to the FDTD method and produced more accurate and efficient results.

Keywords: Overlapping Grid Method; Spline Interpolation; scattering technique; object reconstruction

INTRODUCTION

Microwave imaging attracted significant interest among researchers due to its unique features as an excellent diagnostic tool or as a practical resource in several areas. For example, the microwave is primarily used for ground-penetrating radar (Catapano, Gennarelli, Ludeno & Soldovieri 2019; Zhou, Chen, Lyu, & Chen 2022), geophysical exploration (Rosa, Bergmann, & Teixeira, 2020), buried object detection (Wee 2020), and medical diagnostic (Dachena et al. 2020; Stancliff 2017; Salleh et al. 2020).

Active microwave imaging is a wave-based non-invasive imaging method involving two principles; tomographic and confocal radar. Microwave tomography is divided into two categories: qualitative and quantitative imaging. The qualitative microwave imaging method generates a qualitative profile, such as a reflectivity feature or a qualitative picture representing a hidden item. The quantitative imaging approach is used to obtain the electrical and magnetic properties distribution to obtain the geometrical parameters of an imaged object. The spatial distribution of the complex permittivity is calculated using the transmitted (incident) and received (scattered) fields (Nikolova 2011).
The FDTD algorithm is a simple and effective way of addressing Electromagnetic (EM) interaction problems (Baek, Kim, & Jung 2018; Rahman & Rather 2020). Moreover, it can analyse a wide range of frequencies without using additional computer resources. Therefore, the time-domain inversion method is suitable for improving the detection and reconstruction of embedded objects (Narayan 2017; Okada 2014; Schneide 2016). However, this algorithm is limited to intrinsic orthogonal grids due to it is based on a Cartesian coordinate system. Hence, it is challenging to build the meshes for modelling curved borders and microscopic structures (E. Jiménez-Mejía, & Herrera-Murcia, J. 2015; Nilavalan 2002). Several approaches for improving the efficiency of the FDTD method have been published in the literature, including non-uniform (E. Jiménez-Mejia & Herrera-Murcia 2015), sub-gridding (Cabello et al. 2017), and sub-cell algorithm (Navarro et al. 2021). Nevertheless, those approaches still have some disadvantages, such as requiring a long calculation time and additional memory, as well as the Courant-Friedrichs-Lewy (CFL) stability requirement restricting time step or cell size (De Moura & Kubrusly 2013).

Therefore, an Overlapping Grid Method (OGM) with Biquadratic Spline Interpolation in Forward-Backward Time Stepping (FBTS) Technique was proposed and developed in this paper. In order to calculate the dispersed fields for an embedded object, two-dimensional (2D) numerical simulations for electromagnetic (EM) field analysis in various ratios for the sub-grid were carried out. Then, the proposed method incorporated the FBTS inverse scattering technique for detecting and reconstructing embedded objects with different shapes. Finally, the efficiency of the proposed method was examined by Mean Square Error (MSE) and by normalizing the functional error.
An Overlapping Grid method is a grid embedding technique that provides a theoretically direct domain decomposition mechanism (Yang, Shao, Li, & Chen 2019). This method divides the computing domain into two or more subdomains in the measured EM region. The advantages of an Overlapping Grid method are it can reduce complex geometric problems and produce the quality and spatial resolution of imaging. An Overlapping grid comprises two grids, as seen in Figure 1(a). The Finite-difference time-domain (FDTD) lattice, also known as Layer 1 (main-grid), is utilized to cover the whole computational domain. Layer 2 (sub-grid) is an overlapping field used to model an undefined numerical entity. The Biquadratic Spline interpolation approach will be used to determine the overlapping region between the main-grid and the sub-grid. The area where the main-grid and sub-grid overlap can be determined by using Biquadratic Spline Interpolation. Then, unknown values at the border points can be retrieved in the overlapping region. Biquadratic Spline interpolation (Boor, 1978; Schumaker, 2015; Späth, 1995) will provide more accurate results due to the fact that it is constructing new data points within the range of a discrete set of known data points (Han 2013; Singh 2016). As a result, it can generate more accurate interpolation for determining curved borders and microscopic features.

Figure 1(b) depicts a four (4) point Biquadratic Spline interpolation derived from Figure 1(a). P, Q, R, and S are the four known value points from the main-grid, whereas Z' is an unknown value point from the sub-grid. The unknown value of Z'(x sub, y sub) is interpolated by using the A(x a, y a) and B(x b, y b) at the y-axis as in Equation (1).

\[
Z' = \left[ \frac{D_{j,1} - D_j}{2(y_j - y_0)} \right] (y_j - y_0) + d_j (y_j - y_0) + A
\]

\[
j = 0, 1, 2, ..., M
\]

where,

\[
D_j = 0, \quad D_{j,1} = 2(B - A) \frac{(y_j - y_0)}{x_j - x_0} - D_j, \quad j = 0, 1, 2, ..., M
\]

\[
A = \left[ \frac{D_{j,1} - D_j}{2(x_j - x_0)} \right] (x_j - x_0) + D_j (x_j - x_0) + P
\]

\[
\therefore D_j = 0, \quad D_{j,1} = 2(Q - P) \frac{(x_j - x_0)}{x_j - x_0} - D_j, \quad i = 0, 1, 2, ..., N
\]

\[
B = \left[ \frac{D_{j,1} - D_j}{2(x_j - x_0)} \right] (x_j - x_0) + D_j (x_j - x_0) + R
\]

\[
\therefore D_j = 0, \quad D_{j,1} = 2(S - R) \frac{(y_j - y_0)}{y_j - y_0} - D_j, \quad i = 0, 1, 2, ..., N
\]

**DIRECT AND INVERSE SCATTERING TECHNIQUE**

There are two types of electromagnetic scattering problems: direct and inverse scattering. The distribution of dispersed fields can be calculated using the direct scattering technique. In contrast, the inverse scattering issue is used to deduce an object’s attributes (e.g., structure, location, and dielectric properties) based on scattered field measurement findings.

Direct scattering formulates the problem in the time or frequency domain using microwave signals. As seen in Figure 2, direct scattering is used to calculate an object’s dispersed area using two antennas. In free space, the target is implanted with transmitter (T) and reception (R) antennas inside the Region of Interest (ROI). Each antenna sequentially broadcasts microwave signals, while the remaining antennas act as receivers, absorbing scattered fields.

Colton and Kress (Colton 1998) defined the inverse scattering problem as an inverse problem that was highly difficult to solve. However, this scattering problem can be solved by using Forward-Backward Time Stepping (FBTS) technique (Takenaka 2015), as illustrated in Figure 3. The FBTS technique can reconstruct an image based on its electrical characteristics for solving the nonlinear inverse problem.

Microwave tomography collects information about an object by sending microwave pulses and dispersed pulses for data analysis, also known as a computationally intensive image reconstruction algorithm. The overlapping grid method with the FBTS scattering technique is described in detail in (Wee 2020).
OGM method with Spline Interpolation in FBTS Inverse Scattering Technique

Start

Parameters setting

Measurement setup
i. Create or load image for simulation
ii. Transmitter and Receiver antennae setting

Direct Scattering
i. Interpolate the EM field by using Biquadratic Spline interpolation in OGM lattice
ii. Measured the EM fields for an arbitrary shaped multiple objects in time-domain

Iteration

Forward Scattering
i. Forward time-stepping setup
ii. Each antenna serves as a transmitter that send pulses one at a time, while the other 15 antennas take on the role of receivers that collect the dispersed electromagnetic fields until a set of transmitter or receiver data for 16 antenna combinations was produced.
iii. Interpolate the EM field by using OGM with Biquadratic spline interpolation
iv. Measure and store the reconstruction data in Forward scattering

Backward Scattering
i. Backward time-stepping setup
ii. Each antenna serves as a transmitter that send pulses one at a time, while the other 15 antennas take on the role of receivers that collect the dispersed electromagnetic fields until a set of transmitter or receiver data for 16 antenna combinations was produced.
iii. Interpolate the EM field by using OGM with Biquadratic spline interpolation
iv. Measure and store the reconstruction data in Backward scattering

Calculate the Gradient and Search Direction

Update estimated profile and calculate the Cost Functional

When iteration = Number of iteration

Plot the two dimensional reconstruction images (Relative Permittivity and Conductivity)

Change parameters setting for Initial guess value and frequency

Next iteration

No Satisfactory

Yes

End

FIGURE 4. Flow chart for proposed numerical method
The OGM with Biquadratic Spline Interpolation in FBTS Inverse Scattering algorithm is shown in Figure 4. All parameters needed for this simulation were specified, and values were assigned. The measuring procedure for the dispersed field was then established. The dielectric characteristics of embedded objects and the Region of Interest (ROI) were included in the actual profiles. In the simulations, an excitation signal was a sinusoidal modulated Gaussian pulse. Each antenna functioned as a transmitter, successively transmitting a pulse, while the remaining 15 antennas served as receivers, collecting dispersed electromagnetic fields.

FBTS is a technique for determining important quantitative information about embedded objects. The forward step begins with applying a Gaussian pulse signal to the predicted profile of an embedded object. Then, the dispersed fields for forwarding time-stepping were calculated by using the OGM approach. In the OGM lattice, the EM field was interpolated using Biquadratic Spline Interpolation for the overlapped region. The forward time-stepping reconstructions data gathered at the receiving location was then compared to the measurement data.

The adjoint fields with backward time-stepping were calculated by using the OGM with Biquadratic Spline Interpolation where there was backward scattering. Data from the receiving point’s backward time-stepping reconstructions were gathered and compared to measurement data. Finally, the original profile was irradiated with the difference between the observed and estimated scattered fields as a source.

The cost functional was utilized to reduce the number of FBTS reconstruction iterations. It was calculated by comparing the estimated and actual profiles. Finally, MATLAB was used to illustrate the reconstructed relative permittivity and conductivity images in the two-dimensional. Mean Square Error (MSE) was used to compare the reconstructed image with the original image to evaluate the accuracy of the proposed method.

RESULTS AND DISCUSSION

This paper focuses on the development of the OGM with spline interpolation and demonstrates its efficiency. We have previously published the study related to the noise for the proposed inverse scattering technique in (Elizabeth et al., 2015; Munawwarah Ibrahim et al., 2016). In this research, a study on the performance of OGM with spline interpolation in direct and inverse scattering was evaluated in Case A, Case B and Case C.

A 2D numerical model was used to analyse the effectiveness of the OGM with the spline interpolation technique in a direct scattering process. The spline interpolation technique will transfer the data between the main-grid and the sub-grid. Figure 5 shows the sub-grid was configured to converge on top of the main-grid, with \( L_s \) and \( W_s \) denoting the length and width for sub-grid, respectively. \( L_m \) and \( W_m \) are the length and width of the main-grid, respectively. The values of \( L_s, W_s, L_m \) and \( W_m \) were consistent with \((i, j)\) and \((m, n)\). In this study, the sub-grid was set to 50 mm x 50 mm grids, while the main-grid was set to 190 mm x 190 mm grids. In addition, the cell size was set to 1 mm x 1 mm for the main-grid and the sub-grid.

Two (2) antennas are utilized in this work at a distance of 170 mm. The transmitter antenna will broadcast a signal, while the receiver antenna will collect the dispersed field. The excitation signal was a sinusoidal modulated Gaussian pulse with a core frequency of 2.0 GHz and a bandwidth of 1.3 GHz. This pulse was stimulated into the Overlapping lattice by the transmitter. The main grid was encircled by a Convolution Perfectly Matched Layer (CPML) with a thickness of 15 mm. It is used to eliminate signal reflection at the boundary of the environment. Table 1 presents the dielectric profile setting in free space.

<table>
<thead>
<tr>
<th>Layer</th>
<th>Class</th>
<th>Size</th>
<th>( \varepsilon_r ) (F/m)</th>
<th>( \sigma ) (S/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main-grid</td>
<td>Background</td>
<td>190 mm x 190 mm</td>
<td>1.00</td>
<td>0.00</td>
</tr>
<tr>
<td>ROI Region</td>
<td></td>
<td>50 mm (radius)</td>
<td>1.00</td>
<td>0.00</td>
</tr>
<tr>
<td>Sub-grid</td>
<td>Square Object</td>
<td>50 mm x 50 mm</td>
<td>1.00</td>
<td>0.00</td>
</tr>
</tbody>
</table>
CASE A(1): VALIDATION OF ACCURACY BY SPACE INCREMENT OF SUB-GRADE WITH A DIRECT SCATTERING

Figure 5 shows the numerical model of the Overlapping method with spline interpolation in free space. The observation point is in the middle of the sub-grid and main-grid. The spaces of main-grid, $\Delta x_m$ and $\Delta y_m$ were set as $\Delta x_m = \Delta y_m = 1$ mm. The space of the sub-grid was set as $\Delta x_s = \Delta y_s = 1$ mm and used as references in this analysis.

The spacing increment of the sub-grid, $\Delta x_s$ was changed from 1.2 mm to 2.0 mm to examine an accuracy of the proposed method in direct scattering. However, the $\Delta y_s$ was maintained at 1 mm. Figure 6 shows the absolute error of the amplitude of $E_z$ field versus the space increment of sub-grid, $\Delta x_s$. It was discovered that the absolute error of the amplitude of the $E_z$ field increased when the $\Delta x_s$ increased. As a result, smaller grid spacing or cell sizes have produced more accurate findings.

CASE A(2): VALIDATION OF ACCURACY BY RATIO OF THE GRID SIZE WITH DIRECT SCATTERING

A range of ratios of the grid size, $R$ between the main-grid and sub-grid, was utilized to investigate the precision of the proposed numerical method. As shown in Figure 6, the ratios of the grid size among the main grid and the sub-grid were $R = \left( \frac{L_s}{L_m} \right) / \left( \frac{L_m}{L_m} \right)$. In this analysis, the number of grids on the main grid, $I_{m(m)} \times I_{m(m)}$ were fixed to 190 mm x 190 mm grids. The number of the grids on the sub-grid $I_{s(i)} \times I_{s(j)}$ were set based on Table 2. The number of grids in the sub-grid decreased when the ratio of grid size increased. The ratio of grid size, $R = 1.0$ and number of the grids $I_{s(i)} \times I_{s(j)} = 50$ mm x 50 mm for sub-grid were used as a reference in this analysis. All these simulations were carried out in free space.

### Table 2. The ratio of grid sizes between 0.1 until 0.7

<table>
<thead>
<tr>
<th>Ratio</th>
<th>Number of grids for sub-mesh, $I_{s(i)} \times I_{s(j)}$ (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>500 x 500</td>
</tr>
<tr>
<td>0.2</td>
<td>250 x 250</td>
</tr>
<tr>
<td>0.3</td>
<td>166 x 166</td>
</tr>
<tr>
<td>0.4</td>
<td>125 x 125</td>
</tr>
<tr>
<td>0.5</td>
<td>100 x 100</td>
</tr>
<tr>
<td>0.6</td>
<td>83 x 83</td>
</tr>
<tr>
<td>0.7</td>
<td>71 x 71</td>
</tr>
</tbody>
</table>

Figure 7 illustrates the computing time versus grid size ratio for sub-grid. The computational time decreased when the ratio of grid size increased. The results showed that the smallest grid size ratio required the highest computational time.

Figure 8 depicts the number of steps versus the amplitude of $E_z$ field.
Figure 8 shows the amplitude of $E_z$ field with a different ratio of grid size versus the number of steps. The solid line colour (red, yellow, green, cyan, blue, purple, and dark) represented the ratio of the grid, $R = 0.1$ until 0.7. Figure 9 shows the maximum amplitude of $E_z$ field versus the ratio of grid size. It was found that the maximum amplitude of $E_z$ field increased as the grid size ratio increased.

The absolute error, $\text{Absolute Error} = |E_R(t) - E_{R_{1.0}}(t)|$ was used to examine the error analysis for a received signal at the observation point, where $E_{R_{1.0}}(t)$ is an electric field in an overlapping lattice for $R=0.1$ as the benchmark, and $E_R(t)$ is an electric field in an overlapping lattice for $R$ values ranging from 0.1 to 0.7. Figure 10 depicts the absolute inaccuracy of the amplitude of the $E_z$ field versus the grid size ratio. The findings revealed that as the grid size ratio increased, the absolute error of the amplitude $E_z$ also increased. Consequently, it may be stated that a more refined grid size can yield more accurate findings.

CASE B: ANALYSING ELECTROMAGNETIC FIELD FOR AN EMBEDDED OBJECT IN A DIELECTRIC MEDIUM

In case B, the numerical model configuration for an embedded object was created based on Figure 5. The dielectric characteristics were established in accordance with Table 3. The dispersed fields for an embedded object were examined with error analysis to examine the stability and effectiveness of the OGM approach with spline interpolation.

<table>
<thead>
<tr>
<th>Layer</th>
<th>Class</th>
<th>Size</th>
<th>$\varepsilon_r$ (F/m)</th>
<th>$\sigma$ (S/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main-grid</td>
<td>Background</td>
<td>190 mm x 190 mm</td>
<td>1.00</td>
<td>0.00</td>
</tr>
<tr>
<td>ROI Region</td>
<td></td>
<td>50 mm (radius)</td>
<td>9.98</td>
<td>0.18</td>
</tr>
<tr>
<td>Sub-grid</td>
<td>Square Object</td>
<td>50 mm x 50 mm</td>
<td>35.26</td>
<td>1.13</td>
</tr>
</tbody>
</table>

The comparison of transmitted and received signals for embedded objects in free space using the FDTD method, OGM with the Bilinear Interpolation, and OGM with the Spline Interpolation is shown in Figures 11 and 12.
In order to analyze the efficiency of the proposed method, the error analysis for received signal was investigated by using relative error, \[ \text{Relative Error} = \frac{|E_z(t) - E_0(t)|}{E_0(t)} \] and Mean Square Error (MSE), \[ \text{MSE} = \frac{1}{N} \sum_{t=1}^{N} (E_z(t) - E_0(t))^2, \] where, \( E_0(t) \) is the electric field in FDTD lattice, \( E_z(t) \) is the electric field in OGM with bilinear interpolation or OGM with spline interpolation, and \( N \) is the total number of time steps.

**TABLE 4. Error analysis for received signal in Case B**

<table>
<thead>
<tr>
<th>OGM with the bilinear interpolation technique</th>
<th>OGM with the spline interpolation technique</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum amplitude peak of ( E_z ) (V/m)</td>
<td>1.11278 \times 10^{-4}</td>
</tr>
<tr>
<td>Relative error (%)</td>
<td>9.5%</td>
</tr>
<tr>
<td>MSE (10^{-10})</td>
<td>1.8759 \times 10^{-10}</td>
</tr>
<tr>
<td></td>
<td>1.87406 \times 10^{-10}</td>
</tr>
</tbody>
</table>

Table 4 presents the error analysis for received signals in free space. The maximum amplitude peak of electric field, \( E_0(t) \) for FDTD method was \( 1.01627 \times 10^{-4} \) and is used as a reference in this analysis. This is due to the difference between OGM method with bilinear interpolation and OGM method with spline interpolation can be compared and analyzed. The OGM method with spline interpolation showed lower relative error than the OGM method with bilinear interpolation of difference. Besides, the MSE for the OGM method with spline interpolation was also lower than the OGM method bilinear interpolation based on Table 4. Hence, it proves that the OGM method with spline interpolation could to measure the scattered fields around an embedded object accurately as compared with OGM method with bilinear interpolation.

**CASE C: RECONSTRUCTION OF EMBEDDED MULTIPLE OBJECTS WITH INVERSE SCATTERING**

Figure 13 illustrates the numerical model of microwave tomography for the square object in 2D. Layer 1 was equipped with 190 mm x 190 mm grids. Layer 2 was configured with 50 mm x 50 mm grids. The sub-grid was created as multiple objects and located on top of the main grid with cell size, \( \Delta x = 1 \) mm and \( \Delta y = 1 \) mm. The ROI region was immersed in free space as the backdrop media. A sinusoidal modulated Gaussian pulse with a core frequency of 2.0GHz and a bandwidth of 1.3 GHz was utilized in this work as an excitation signal. The ROI was irradiated by sixteen (16) point source antennas. Each point source antenna served as a transmitter, generating one Gaussian pulse at a time. The remaining fifteen (15) antennas were converted into receivers to collect dispersed fields in the main lattice. Gradient optimization was used up to 100 iterations to reconstruct the microwave image and minimize the functional error.

![Figure 13. The numerical model of multiple embedded objects](image)

The electrical profiles for the numerical model of multiple objects are summarised in Table 5. The dielectric characteristics of ROI represent fatty tissues, and the square object is assumed to represent fibroglandular tissues in the breast. The main-backdrop lattices are supposed to be free space.

**TABLE 5. Dielectric Profiles Setting**

<table>
<thead>
<tr>
<th>Layer</th>
<th>Class</th>
<th>Size</th>
<th>( \varepsilon_r ) (F/m)</th>
<th>( \sigma ) (S/m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Main grid</td>
<td>Background</td>
<td>190 mm x 190 mm</td>
<td>1.00</td>
<td>0.00</td>
</tr>
<tr>
<td>Sub-grid</td>
<td>ROI 50 mm (radius)</td>
<td>9.98</td>
<td>0.18</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Circular Object</td>
<td>10 mm (radius)</td>
<td>21.45</td>
<td>0.46</td>
</tr>
<tr>
<td></td>
<td>Square Object</td>
<td>20 mm x 20 mm</td>
<td>21.45</td>
<td>0.46</td>
</tr>
</tbody>
</table>

Figure 14 depicts the real dielectric profiles of multiple simple-shaped objects. Figure 15 demonstrates the reconstructed dielectric profiles of the FDTD method in FBTS and it was used as a reference in this analysis. The FDTD approach in FBTS is limited to intrinsic orthogonal grids because it cannot describe curved borders and minor characteristics of several basic objects. Therefore, an Overlapping Grid Method with scattering technique was proposed in this case study. Figure 16 shows the reconstructed dielectric profiles of the proposed algorithm. The proposed algorithm effectively reconstructed the dielectric profiles of the circular and square objects. The findings present that the proposed algorithm can generate more accurate and efficient interpolation in the reconstruction images to detect curved borders and minor features.
FIGURE 14. Real dielectric profiles

(a) Real relative permittivity
(b) Real conductivity

FIGURE 15. Reconstructed dielectric profiles for FDTD method in FBTS

(a) Reconstructed relative permittivity
(b) Reconstructed conductivity

FIGURE 16. Reconstructed dielectric profiles for proposed method

(a) Reconstructed relative permittivity
(b) Reconstructed conductivity
Figure 17 and Figure 18 show a 1D cross-section of the original and reconstructed dielectric profiles. Cross-sectional views of the actual and reconstructed dielectric profiles for a circular embedded object are shown in Fig. 15, while for a square embedded object are shown in Fig. 16. These images show the stark difference in dielectric characteristics between the buried items and ROI. The findings demonstrated that the proposed numerical method could distinguish between square and circular objects in ROI while estimating dielectric values accurately.

The proposed method’s efficacy was assessed by using the Mean Square Error (MSE), as shown in Table 6. According to this investigation, the MSE of reconstructed dielectric profiles utilizing the proposed method produced much lower values than the FDTD method in FBTS. The relative permittivity profile differed by 27.06%, whereas the conductivity profile differed by 20%.

<table>
<thead>
<tr>
<th>Methods</th>
<th>Relative Permittivity MSE</th>
<th>Conductivity MSE</th>
</tr>
</thead>
<tbody>
<tr>
<td>FDTD approach in FBTS</td>
<td>1.6618</td>
<td>$9.8572 \times 10^{-4}$</td>
</tr>
<tr>
<td>Overlapping grid Method with Biquadratic Spline Interpolation in FBTS</td>
<td>$1.2120$</td>
<td>$7.8851 \times 10^{-4}$</td>
</tr>
</tbody>
</table>

Figure 19 depicts the normalized functional error vs iterations count. A gradient optimization with 100 iterations was used to reconstruct the numerous simple-shaped objects. As observed, the normalized functional error was reduced as the number of iterations increased. It was also discovered that in FBTS, the OGM with Biquadratic Spline Interpolation showed lower values of normalised functional error than the FDTD approach.
At 100th iterations, the difference in normalised functional error between these two techniques was $1.41 \times 10^{-7}$. Compared to the FDTD approach in FBTS, the results showed that the proposed method could accurately reconstruct numerous simple-shaped objects. Consequently, the proposed method successfully addressed a recognized problem in the FDTD method. It was challenging to simulate the curving borders and tiny features due to inherent orthogonal grid restrictions.

CONCLUSION

An Overlapping Grid Method with Biquadratic Spline Interpolation in direct scattering method was proposed as a new numerical method for measuring the scattered fields around an embedded object. The findings show that smaller grid spacing or cell sizes can produce more accurate results. The results also indicated that when the grid size ratio increases, the absolute error of the amplitude $E_z$ will also be increased. Consequently, it may be stated that a more refined grid size can yield more accurate findings. The FBTS inverse approach was combined with the Overlapping Grid Method with Biquadratic Spline Interpolation to solve inverse scattering issues. The findings demonstrated that the proposed technique was excellent at recognizing buried items and rebuilding them into various forms. As opposed to the FDTD method in FBTS, the proposed approach generates sharper and better-reconstructed images.

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DECLARATION OF COMPETING INTEREST

None


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