

## FLOW OVER A STRETCHING SHEET IN A MICROPOLAR FLUID WITH RADIATION EFFECT

(Aliran pada Helaiian Meregang dalam Bendalir Mikroktub dengan Kesan Sinaran)

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### ABSTRACT

Boundary layer flow and heat transfer characteristics induced by a linearly stretching sheet immersed in an incompressible micropolar fluid with prescribed surface heat flux in the presence of radiation effect is investigated. The governing system of partial differential equations is first transformed into a system of ordinary differential equations using similarity transformation, which are then solved numerically using the Runge-Kutta-Fehlberg method. The velocity, angular velocity and temperature profiles with the effects of various physical parameters are presented graphically. It is found that the heat transfer rate at the surface decreases in the presence of radiation.

*Keywords:* boundary layer; heat transfer; micropolar fluid; radiation; stretching sheet

### ABSTRAK

Ciri-ciri aliran lapisan sempadan dan pemindahan haba yang dirangsang oleh helaiian meregang secara linear dalam bendalir mikroktub tak mampat dengan fluks haba permukaan ditetapkan dan dengan kehadiran kesan sinaran diselidik. Sistem persamaan menakluk dalam bentuk persamaan pembezaan separa dijelmakan kepada sistem persamaan pembezaan biasa menggunakan penjelmaan keserupaan, yang seterusnya diselesaikan secara berangka menggunakan kaedah Runge-Kutta-Fehlberg. Profil-profil halaju, halaju sudut dan suhu dengan pelbagai kesan parameter fizikal dipersembahkan dalam bentuk graf. Didapati kadar pemindahan haba pada permukaan menyusut dengan kehadiran sinaran.

*Kata kunci:* lapisan sempadan; pemindahan haba; bendalir mikroktub; sinaran; helaiian meregang

### References

- Abramowitz M. & Stegun I.A. 1965. *Handbook of Mathematical Functions*. New York: Dover.
- Afzal N. 1993. Heat transfer from a stretching surface. *Int. J. Heat Mass Transfer* **36**: 1128-1131.
- Ahmadi G. 1976. Self similar solution of incompressible micropolar boundary layer flow over a semi-infinite flat plate. *Int. J. Eng. Sci.* **14**: 639-646.
- Ali M.E. 1994. Heat transfer characteristics of a continuous stretching surface. *Heat Mass Transfer* **29**: 227-234.
- Ali M.E. 1995. On thermal boundary layer on a power-law stretched surface with suction or injection. *Int. J. Heat Fluid Flow* **16**: 280-290.
- Brewster M.Q. 1992. *Thermal Radiative Transfer Properties*. New York: John Wiley and Sons.
- Chen C.K. & Char M.I. 1988. Heat transfer of a continuous stretching surface with suction and blowing. *J. Math. Anal. Appl.* **135**: 568-580.
- Crane L.J. 1970. Flow past a stretching plate. *Z. Angew. Math. Phys.* **21**: 645-647.
- Datti P.S., Prasad K.V., Abel M.S. & Joshi A. 2004. MHD viscoelastic fluid flow over a non-isothermal stretching sheet. *Int. J. Eng. Sci.* **42**: 935-946.
- Dutta B.K., Roy P. & Gupta A.S. 1985. Temperature field in the flow over a stretching sheet with uniform heat flux. *Int. Commun. Heat Mass Transfer* **12**: 89-94.

- Elbarbary E.M.E. & Elgazery N.S. 2004. Chebyshev finite difference method for the effects of variable viscosity and variable thermal conductivity on heat transfer from moving surfaces with radiation. *Int. J. Thermal Sci.* **43**: 889-899.
- Grubka L.J. & Bobba K.M. 1985. Heat transfer characteristic of a continuous, stretching surface with variable temperature. *ASME J. Heat Transfer* **107**: 248-250.
- Gupta P.S. & Gupta A.S. 1977. Heat and mass transfer on a stretching sheet with suction or blowing. *Can. J. Chem. Eng.* **55**: 744-746.
- Hayat T., Abbas Z. & Javed T. 2008. Mixed convection flow of a micropolar fluid over a non-linearly stretching sheet. *Phys. Lett. A* **372**: 637-647.
- Ishak A. 2009. Thermal boundary layer flow over a stretching sheet in a micropolar fluid with radiation effect. *Meccanica* online first DOI 10.1007/s11012-009-9257-4.
- Khan S.K. 2006. Heat transfer in a viscoelastic fluid flow over a stretching surface with heat source/sink, suction/blowing and radiation. *Int. J. Heat Mass Transfer* **49**: 628-639.
- Mahmoud M.A.A. 2007. Thermal radiation effects on MHD flow of a micropolar fluid over a stretching surface with variable thermal conductivity. *Physica A* **372**: 401-410.
- Muthucumaraswamy R. & Chandrakala P. 2005. Effects of thermal radiation on moving vertical plate in the presence of an optically thin gray gas. *Forsch Ingenieurwes* **69**: 205-208.
- Nazar R., Amin N. & Pop I. 2004. Stagnation point flow of a micropolar fluid towards a stretching sheet. *Int. J. Non-Linear Mech.* **39**: 1227-1235.
- Raptis A. & Perdikis C. 1999. Radiation and free convection flow past a moving plate. *Int. J. Appl. Mech. Eng.* **4**: 817-821.
- Raptis A. 1998. Flow of a micropolar fluid past a continuously moving plate by the presence of radiation. *Int. J. Heat Mass Transfer* **41**: 2865-2866.
- Siddheswar P.G. & Mahabaleswar U.S. 2005. Effects of radiation and heat source on MHD flow of a viscoelastic liquid and heat transfer over a stretching sheet. *Int. J. Non-Linear Mech.* **40**: 807-820.

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