

## PEMODELAN DINAMIK FITOPLANKTON MENGGUNAKAN MODEL NUTRIEN-FITOPLANKTON-ZOOPLANKTON

(Dynamic Modelling of Phytoplankton using Nutrient-Phytoplankton-Zooplankton Model)

NADIAH ABU BAKAR<sup>1</sup>, ROKIAH@ROZITA AHMAD<sup>2</sup>, AZMIN SHAM RAMBELY<sup>3</sup> &  
SHUHAIMI-OTHTMAN M.<sup>4</sup>

### ABSTRAK

Kadar pertumbuhan fitoplankton yang berlebihan boleh membawa impak yang negatif kepada ekosistem di Tasik Chini. Walau bagaimanapun, fitoplankton merupakan komponen penting dalam jaringan makanan akuatik. Oleh itu, kajian terhadap kepekatan fitoplankton dalam Tasik Chini adalah penting agar dapat memantau keadaan ekosistem tasik. Kajian ini bertujuan untuk membangunkan model matematik dinamik yang sesuai bagi fitoplankton di Tasik Chini dengan menggunakan model nutrien-fitoplankton-zooplankton, serta untuk mengenal pasti bahawa input nutrien adalah faktor kawalan bagi model ini. Persamaan pembezaan biasa (PPB) digunakan untuk simulasi model fitoplankton di Tasik Chini. Model fitoplankton ini terdiri daripada kepekatan nutrien ( $Nu$ ), fitoplankton ( $F$ ) dan zooplankton ( $Z$ ). Sistem PPB ini diselesaikan dengan kaedah Runge-Kutta-Fehlberg, menggunakan perisian Maple 13. Model  $NuFZ$  yang dibangunkan ini memilih input nutrien sebagai parameter bifurkasi, iaitu model ini dikawal oleh input nutrien. Hasil kajian menunjukkan bahawa kesan daripada peningkatan input nutrien ke dalam sistem tasik telah menyebabkan sistem menjadi tidak stabil dan kepadatan fitoplankton berubah-ubah. Model ini berguna untuk membantu dalam pemahaman populasi fitoplankton di Tasik Chini.

*Kata kunci:* Persamaan pembezaan biasa; model fitoplankton; Tasik Chini

### ABSTRACT

The widespread growth rate of phytoplankton can cause negative impact to the ecosystem in Tasik Chini. However, phytoplankton are important component in the aquatic food web. Thus, the study on the concentration of phytoplankton in Tasik Chini is essential in order to monitor the ecosystem of the lake. The aim of this study is to develop appropriate dynamic mathematical model of phytoplankton in Tasik Chini by using nutrient-phytoplankton-zooplankton model and to determine the nutrient input as the controlling factor in this system. Ordinary differential equations (ODE) are used to simulate the model of phytoplankton in Tasik Chini. The phytoplankton model is governed by the concentration of nutrient ( $Nu$ ), phytoplankton ( $F$ ) and zooplankton ( $Z$ ). The ODE system settled down by using Runge-Kutta-Fehlberg method with Maple 13.  $NuFZ$  model is developed by choosing nutrient input as bifurcation parameter, that is the model is nutrient controlled. The results show that the lake system becomes unstable and the phytoplankton density start to oscillate when nutrient input in the system is increasing. This model is useful in assisting the understanding of phytoplankton populations in Tasik Chini.

*Keywords:* Ordinary differential equations; phytoplankton model; Tasik Chini

### Rujukan

- Ali H. 2008. Pemodelan persamaan kadar kepekatan oksigen terlarut dan permintaan oksigen biokimia di Tasik Chini menggunakan kaedah tersirat Crank-Nicolson:1-Matra. Tesis S.Sn, Universiti Kebangsaan Malaysia.
- Armstrong R.A. 1994. Grazing limitation and nutrient limitation in marine ecosystems: Steady state solutions of an ecosystem model with multiple food chains. *Limnol. Oceanogr* **39**: 597-608.

- Beachapedia. 2012. Red tides and harmful algal blooms. [http://www.beachapedia.org/Red\\_Tides\\_and\\_Harmful\\_Algal\\_Blooms](http://www.beachapedia.org/Red_Tides_and_Harmful_Algal_Blooms) (15 Februari 2012).
- Changjin X. 2011. Bifurcations for a phytoplankton model with time delay. *Electronic Journal of Differential Equations* **2011**(148): 1-8.
- Cropp R., Norbury J. & Braddock R. 2007. Dimethylsulphide, clouds, and phytoplankton: insights from a simple plankton ecosystem feedback model. *Global Biogeochemical Cycles* **21**, 17 pp.
- Edwards A.M. & Brindley J. 1999. Zooplankton mortality and the dynamical behaviour of plankton population models. *Bulletin of Mathematical Biology* **61**(2): 303-339.
- Edwards A.M. & Yool A. 2000. The role of higher predation in plankton population models. *Journal of Plankton Research* **22**(6): 1085-1112.
- Evans G.T. & Parslow J.S. 1985. A model of annual plankton cycles. *Biol. Oceanogr.* **3**: 327-347.
- Fasham M.J.R., Ducklow H.W. & McKelvie S.M. 1990. A nitrogen-based model of plankton dynamics in the oceanic mixed layer. *J. Mar. Res.* **48**: 591-639.
- Fasham M.J.R. 1993. Modelling the marine biota. Dlm. Heimann M. (pnyt.). *The Global carbon Cycle*: hlm. 457-504. Berlin: Springer-Verlag.
- Frost B.W. 1987. Grazing control of phytoplankton stock in the open subarctic Pacific Ocean: a model assessing the role of mesozooplankton, particularly the large calanoid copepods *Neocalanus* spp. *Mar. Ecol. Prog. Ser.* **39**: 49-68.
- Gentleman W.C. & Neuheimer A.B. 2008. Functional responses and ecosystem dynamics: how clearance rates explain the influence of satiation, food-limitation and acclimation. *Journal of Plankton Research* **30**(11): 1215-1231.
- Henderson E.W. & Steele J.H. 1995. Comparing models and observations of shelf plankton. *J. Plankton Res.* **17**: 1679-1692.
- Hofmann E.E. & Ambler J.W. 1988. Plankton dynamics on the outer Southeastern U.S. continental shelf. Part II: A time-dependent biological model. *J. Mar. Res.* **46**: 883-917.
- Jørgensen S.E. 2010. A review of recent developments in lake modelling. *Ecological Modelling* **221**: 689-692.
- Ruan S. 2001. Oscillations in plankton models with nutrient recycling. *Journal of Theoretical Biology* **208**: 15-26.
- Shuhaimi-Othman M. & Lim E.C. 2006. Keadaan eutrofikasi di Tasik Chini, Pahang. *Sains Malaysiana* **35**(2): 29-34.
- Shuhaimi-Othman M., Lim E.C. & Idris M. 2007. Water quality changes in Chini Lake, Pahang, West Malaysia. *Environment Monitoring Assessment* **131**: 279-292.
- Steele J.H. & Frost B.W. 1977. The structure of plankton communities. *Phil. Trans. Roy. Soc. Lond., Ser. B* **280**: 485-534.
- Steele J.H. & Henderson E.W. 1992. The role of predation in plankton models. *J. Plankton Res.* **14**: 157-172.
- Steele J.H. & Henderson E.W. 1993. The significance of interannual variability. Dlm. Evans G.T. & Fasham M.J.R. (pnyt.). *Towards a Model of Ocean Biogeochemical Processes*: hlm. 237-260. Berlin: Springer-Verlag.
- Taylor A.H. & Joint I. 1990. A steady-state analysis of the 'microbial loop' in stratified systems. *Mar. Ecol. Prog. Ser.* **59**: 1-17.
- Toriman M.E., Gasim M.B. & Juahir H. 2004. Application of artificial neural network in water level-discharge relationship of Sg. Gumum-Tasik Chini, Pahang. Dlm. Idris M., Hussin K. & Mohamad A.L. (pnyt.). *Sumber Asli Tasik Chini*: hlm. 89-105. Bangi: Penerbit Universiti Kebangsaan Malaysia.
- USEPA. 1985. *Rates, Constant, and Kinetics Formulations in Surface Water Quality Modeling*. 2<sup>nd</sup> Ed. Athens: USEPA.
- Wroblewski J.S. & Richman J.G. 1987. The non-linear response of plankton to wind mixing events-implications for survival of larval northern anchovy. *Journal of Plankton Research* **9**: 103-123.
- Wroblewski J.S. 1989. A model of the spring bloom in the North Atlantic and its impact on ocean optics. *Limnol. Oceanogr.* **34**: 1563-1571.
- Yuntao Z. 2006. A nutrient-phytoplankton-zooplankton model for classifying estuaries based on susceptibility to nitrogen loads. Tesis S. Sn, University of Michigan.

Pusat Pengajian Sains Matematik  
Fakulti Sains dan Teknologi  
Universiti Kebangsaan Malaysia  
43600 UKM Bangi  
Selangor DE, MALAYSIA  
Mel-e: [nhab188@yahoo.com](mailto:nhab188@yahoo.com)\*, [rozy@ukm.my](mailto:rozy@ukm.my), [asr@ukm.my](mailto:asr@ukm.my)

Pusat Pengajian Sains Sekitaran dan Sumber Alam  
Fakulti Sains dan Teknologi  
Universiti Kebangsaan Malaysia  
43600 UKM Bangi  
Selangor DE, MALAYSIA  
Mel-e: [shuhaimi@ukm.my](mailto:shuhaimi@ukm.my)

\* Penulis untuk dihubungi