Journal of Quality Measurement and Analysis
Jurnal Pengukuran Kualiti dan Analisis

JQMA 9(2) 2013, 37-45

CERTAIN NEW CLASS OF CONCAVE FUNCTIONS DEFINED BY SĂLĂGEAN DIFFERENTIAL OPERATOR

(Kelas Baharu Tertentu bagi Fungsi Cekung yang Ditakrif oleh Pengoperasi Pembezaan Sălăgean)

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ABSTRACT

In this article, we introduce a class of concave analytic functions $S^nC_0(\alpha)$ defined by Sălăgean differential operator. We study some properties like coefficient inequalities, distortion theorems and extreme points for this class.

Keywords: analytic function; concave function; Sălăgean differential operator; coefficient inequalities; distortion theorem; extreme points

ABSTRAK

Dalam makalah ini, suatu kelas fungsi analisis cekung $S^nC_0(\alpha)$ yang ditakrif oleh pengoperasi pembezaan Sălăgean diperkenalkan. Beberapa sifat seperti ketaksamaan pekali, teorem erotan dan titik ekstrem untuk kelas ini dikaji.

Kata kunci: fungsi analisis; fungsi cekung; pengoperasi pembezaan Sălăgean; ketaksamaan pekali; teorem erotan; titik ekstrem

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