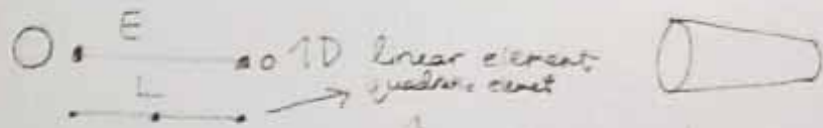


$$M\ddot{U} + KU = F$$

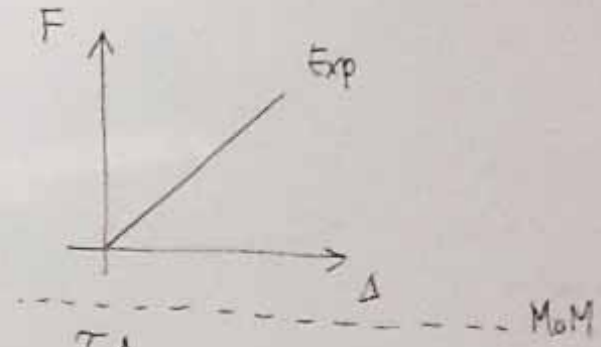
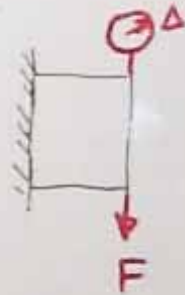


$$\begin{matrix}
 \text{EA} & & & \\
 & -1 & & \\
 \text{L} & & -1 & \\
 & & & 1
 \end{matrix}
 \begin{Bmatrix}
 u_1 \\
 u_2
 \end{Bmatrix}
 =
 \begin{Bmatrix}
 F_1 \\
 F_2
 \end{Bmatrix}$$

unknowns

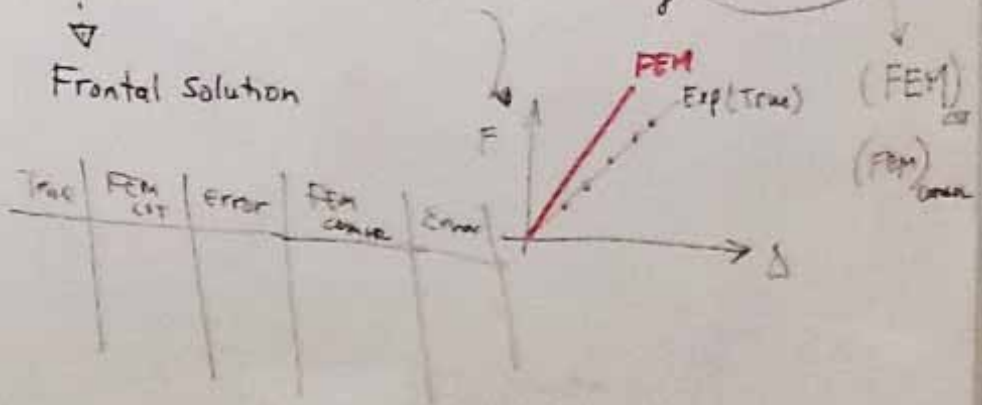
B.C.

Governing Equation / Constitutive Eqⁿ

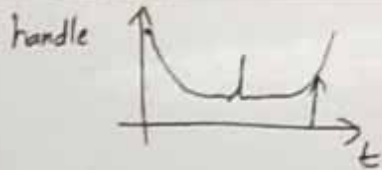


$x = A^{-1}b$
 Gauss Elimⁿ
 ...
 Frontal Solution

$E = f(G, \nu)$
 $E \approx 3G$



True	FEM _{est}	Error	FEM _{conv}	Error



0 → 1
 10 random number

0.2	0.7	0.2
0.4	0.6	0.1
0.1	0.9	0.3
	0.4	

Matlab → Scilab

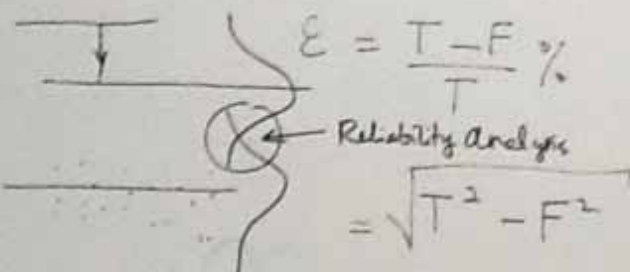
$$\sqrt{x^2 + y^2 + z^2} \quad \varepsilon = T - F$$

$$KU = F$$

$$W = \frac{FL^3}{3(EI)} = \frac{1}{3} \checkmark \#$$

1 ± 0.1

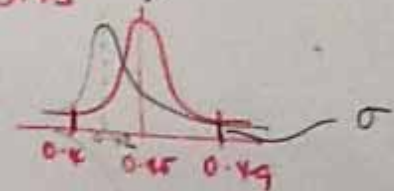
1 ± 0.1



Deterministic → Uncertainty

$$V = 0.4 - 0.49$$

0.45



I

help

www.ukm.my/kamal3/ecm/note1.pdf

$E \pm \varepsilon_e$

$$\frac{EA}{2} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} U = \begin{Bmatrix} F_1 \\ F_2 \end{Bmatrix}$$

$l \pm \varepsilon_x$

3c } force
 3b }
 3g } T

True	F _{ur} FEM	Error	F _{com} FEM	Error

Scilab

rand



Submission

hardcopy — email < 2G
 softcopy — docx

kamal3@gmail.com

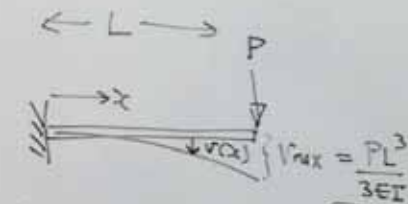
Deterministic

Analytical

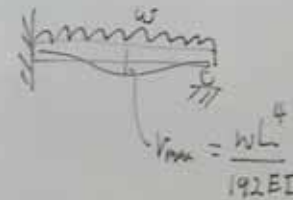
$$v(x) = -\frac{Px^2}{6EI}(3L-x)$$

Finite Element

Uncertainty



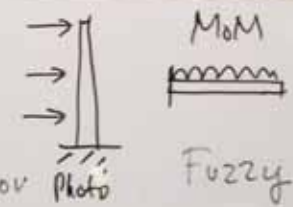
subject P11720 ^{Name} > 2G cloud
 Assignment II
 file name P11720 ^{Name} Assignment II
 Assignment II
 dropbox 5G
 google drive 5G
 box 5G
 15G



Approach

- Probabilistic (Monte Carlo Analysis)
- Non Probabilistic (Fuzzy Analysis)
- Stochastic Approach

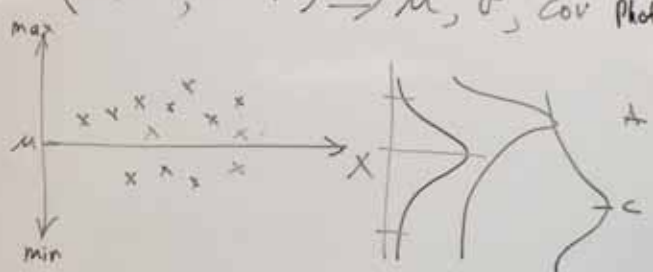
(min, max) ⇒ μ, σ, cov



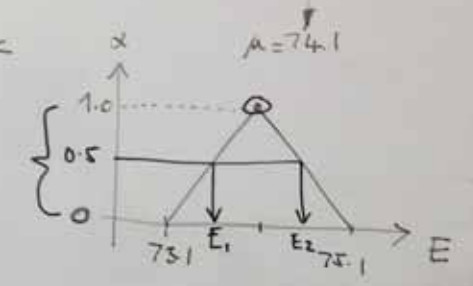
Fuzzy Analysis

Assignment III

Deterministic } Excel
 Monte Carlo } MoM ⇔ Photo
 Fuzzy }
 Stochastic }



* $E = (73.1, 75.1) \text{ MPa } \alpha = 0.5$



- $V = f(E, w_1)$ — ①
 - $f(E, w_2)$ — ②
 - $f(E_2, w_1)$ — ③
 - $f(E_2, w_2)$ — ④
- } min
 } max

$V = f(E, w)$

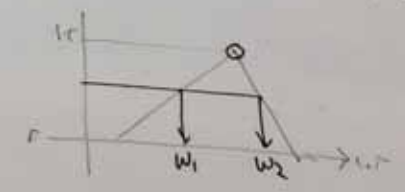
Deterministic $\alpha = 1.0$

$v = f(74.1, 200,000) = *$

Fuzzy $\alpha = 0.5$

$V = \dots$

$w = 80,000 \quad 200,000 \quad 320,000$



$V = (\text{min}, \text{max})$

$\alpha = 0.2$
 $\alpha = 0.8$

